

## Hadronic Mass Moments in $B \rightarrow X_c \ell \nu$ Decays

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## Abstract

We report measurements of the first and second moments of the hadronic invariant mass squared distribution,  $\langle M_X^2 \rangle$  and  $\langle (M_X^2 - \langle M_X^2 \rangle)^2 \rangle$ , in  $B \rightarrow X_c \ell \nu$  decays for minimum lepton momenta ranging from 0.7 to 1.5 GeV/c in the  $B$  meson rest frame. The measurement uses  $B\bar{B}$  events in which the hadronic decay of one  $B$  meson is fully reconstructed and the semileptonic decay of the other  $B$  is inferred from the presence of an identified lepton. These results are obtained from a  $140 \text{ fb}^{-1}$  data sample collected near the  $\Upsilon(4S)$  resonance with the Belle detector at the KEKB asymmetric energy  $e^+e^-$  collider.

Recently, there have been intense theoretical and experimental efforts toward predicting [1, 2, 3, 4] and measuring [5, 6, 7] the moments of the hadronic invariant mass squared distribution in  $B \rightarrow X_c \ell \nu$  decays. The idea is that using the Operator Product Expansion (OPE) [8], the hadronic mass moments (and other inclusive observables in  $B$  decays) can be predicted in terms of the  $b$ -quark mass  $m_b$  and other non-perturbative parameters. Conversely, by measuring the moments of  $B$  decay spectra and the semileptonic  $B$  decay rate, one can then extract these parameters and  $|V_{cb}|$  [9].

The analysis is based on the data recorded with the Belle detector [10] at the asymmetric energy  $e^+e^-$  collider KEKB [11], operating at a center-of-mass (c.m.) energy near the  $\Upsilon(4S)$  resonance. KEKB consists of a low energy ring (LER) of 3.5 GeV positrons and a high energy ring (HER) of 8 GeV electrons. The Belle detector is a large-solid-angle magnetic spectrometer consisting of a three-layer silicon vertex detector (SVD), a 50-layer central drift chamber (CDC), an array of aerogel threshold Čerenkov counters (ACC), a barrel-like arrangement of time-of-flight scintillation counters (TOF), and an electromagnetic calorimeter comprised of CsI(Tl) crystals (ECL) located inside a super-conducting solenoid coil that provides a 1.5 T magnetic field. The responses of the ECL, CDC ( $dE/dx$ ) and ACC detectors are combined to provide clean electron identification. Muons are identified in the instrumented iron flux-return (KLM) located outside of the coil. Charged hadron identification relies on the information from the CDC, ACC and TOF sub-detectors.

The  $\Upsilon(4S)$  dataset used for this study corresponds to an integrated luminosity of  $140 \text{ fb}^{-1}$ , or about 152 million  $B\bar{B}$  events. Another  $15 \text{ fb}^{-1}$  taken 60 MeV below the resonance are used to subtract the non- $B\bar{B}$  (continuum) background. Full detector simulation based on GEANT [12] is applied to Monte Carlo (MC) simulated events. The size of the MC samples is equivalent to about 2.4 times the integrated luminosity. At the generator level, the decay  $B \rightarrow D^* \ell \nu$  is simulated using a HQET-based model [13]. The ISGW2 model [14] is used for the decays  $B \rightarrow D \ell \nu$  and  $B \rightarrow D^{**} \ell \nu$ . The non-resonant  $B \rightarrow D^{(*)} \pi \ell \nu$  component is generated according to the model of Goity and Roberts [15]. QED bremsstrahlung in semileptonic decays is simulated by the PHOTOS package [16].

After selecting hadronic events [17], we fully reconstruct the hadronic decay of one  $B$  meson ( $B_{\text{tag}}$ ) using the decay modes  $B^+ \rightarrow \bar{D}^{(*)0} \pi^+, \bar{D}^{(*)0} \rho^+, \bar{D}^{(*)0} a_1^+$  and  $B^0 \rightarrow D^{(*)-} \pi^+, D^{(*)-} \rho^+, D^{(*)-} a_1^+$  [18]. Pairs of photons satisfying  $E_\gamma > 50 \text{ MeV}$  and  $117 \text{ MeV}/c^2 < m(\gamma\gamma) < 150 \text{ MeV}/c^2$  are combined to form  $\pi^0$  candidates.  $K_S^0$  mesons are reconstructed from pairs of oppositely charged tracks with invariant mass within  $\pm 30 \text{ MeV}/c^2$  of the  $K_S^0$  mass and decay vertex displaced from the interaction point. Candidate  $\rho^+$  and  $\rho^0$  mesons are reconstructed in the  $\pi^+ \pi^0$  and  $\pi^+ \pi^-$  decay modes, requiring their invariant masses to be within  $\pm 150 \text{ MeV}/c^2$  of the  $\rho$  mass. Candidate  $a_1^+$  mesons are obtained by combining a  $\rho^0$  candidate with a charged pion and requiring an invariant mass between 1.0 and  $1.6 \text{ GeV}/c^2$ .  $D^0$  candidates are searched for in the  $K^- \pi^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^+ \pi^-, K_S^0 \pi^+ \pi^-$  and  $K_S^0 \pi^0$  decay modes. The  $K^- \pi^+ \pi^+$  and  $K_S^0 \pi^+$  modes are used to reconstruct  $D^+$  mesons. Charmed mesons are selected in a window corresponding to  $\pm 3$  times the mass resolution in the respective decay mode.  $D^{*+}$  mesons are reconstructed by pairing a charmed meson with a low momentum pion,  $D^{*+} \rightarrow D^0 \pi^+, D^+ \pi^0$ . The decay modes  $D^{*0} \rightarrow D^0 \pi^0$  and  $D^{*0} \rightarrow D^0 \gamma$  are used to search for neutral charmed vector mesons.

For each  $B_{\text{tag}}$  candidate, the beam-constrained mass  $M_{\text{bc}}$  and the energy difference  $\Delta E$  are calculated

$$M_{\text{bc}} = \sqrt{(E_{\text{beam}})^2 - (\vec{p}_B)^2}, \quad \Delta E = E_B - E_{\text{beam}}, \quad (1)$$

where  $E_{\text{beam}}$  is the beam energy in the c.m. system and  $\vec{p}_B$  and  $E_B$  are the 3-momentum and

the energy of the  $B_{\text{tag}}$  candidate in the same frame, respectively. The signal region for  $B_{\text{tag}}$  is defined by the selections  $M_{\text{bc}} > 5.27 \text{ GeV}/c^2$  and  $|\Delta E| < 50 \text{ MeV}$ . If multiple candidates are found in a single event, the best candidate is chosen based on  $\Delta E$  and other variables.

Semileptonic decays of the other  $B$  meson ( $B_{\text{signal}}$ ) are selected by searching for an identified charged lepton (electron or muon) within the remaining particles in the event. Events with multiple identified leptons are rejected. In the lepton momentum range relevant to this analysis, electrons (muons) are selected with an efficiency of 92% (89%) and the probability to misidentify a pion as an electron (a muon) is 0.25% (1.4%) [19, 20]. For  $B^+$  tags, we require that the lepton has a charge sign compatible with a prompt semileptonic decay ( $Q_\ell \cdot Q_B < 0$ , where  $Q_\ell$  and  $Q_B$  are the charges of the lepton and of  $B_{\text{tag}}$ , respectively). In electron events, we attempt to recover bremsstrahlung photons by searching for a  $E_\gamma < 1 \text{ GeV}$  photon within a  $5^\circ$  cone with respect to the electron direction. If such a photon is found, it is merged with the reconstructed electron candidate.

Charged and neutral particles in the event associated neither with  $B_{\text{tag}}$  nor with the charged lepton are assigned to the hadronic  $X$  system. The missing 4-momentum in the event is calculated, assigning the pion mass to all charged particles except identified kaons,

$$p_{\text{miss}} = (p_{\text{LER}} + p_{\text{HER}}) - p_{B_{\text{tag}}} - p_\ell - p_X , \quad (2)$$

where the indices LER and HER refer to the colliding beams. As only the neutrino in  $B \rightarrow X_c \ell \nu$  should be missing in the event, the missing mass is required to be consistent with zero,  $|M_{\text{miss}}^2| < 3 \text{ GeV}^2/c^4$ . To improve the resolution in  $M_X^2$ , we constrain the neutrino mass to zero,  $p_\nu = (|\vec{p}_{\text{miss}}|, \vec{p}_{\text{miss}})$ , and recalculate the 4-momentum of the  $X$  system,

$$p'_X = (p_{\text{LER}} + p_{\text{HER}}) - p_{B_{\text{tag}}} - p_\ell - p_\nu . \quad (3)$$

The  $M_X^2$  resolution (defined as half width at the half maximum) obtained in this way is about  $800 \text{ MeV}^2/c^4$ .

For the rest of the analysis, the remaining events are divided into four sub-samples, depending on the charge of  $B_{\text{tag}}$  ( $B^+$ ,  $B^0$ ) and on the lepton type (electron, muon). In each of these sub-samples and for each lepton momentum threshold considered in the analysis ( $p_\ell^* > 0.7, 0.9, 1.1, 1.3$  and  $1.5 \text{ GeV}/c$  [21]), the backgrounds in the  $M_X^2$  distribution are determined, taking into account contributions from the following sources: continuum background,  $B\bar{B}$  events with a misreconstructed  $B_{\text{tag}}$  candidate, and background from secondary or fake leptons. The background shapes in  $M_X^2$  are determined from the MC simulation, except for the continuum where the off-resonance data is used. The shape of the fake muon background is corrected by the ratio of the pion fake rate in the experimental data over the same quantity in the MC simulation, as measured using  $K_S^0 \rightarrow \pi^+ \pi^-$  decays. The continuum background is scaled by the on- to off-resonance luminosity ratio, taking into account the cross-section difference. The combinatorial  $B_{\text{tag}}$  background is normalized using the  $5.20 \text{ GeV}/c^2 < M_{\text{bc}} < 5.25 \text{ GeV}/c^2$  sideband. The normalization of the secondary or fake lepton background is found from the real data by fitting the lepton momentum distribution. The purity of the  $B \rightarrow X_c \ell \nu$  signal depends on the sub-sample and the lepton momentum threshold, typical values being around 75%. Table I shows the numbers of signal events and purities for each combination of  $B_{\text{tag}}$  charge, lepton type and lepton momentum threshold.

In each of the four sub-samples and for each lepton momentum threshold, the  $M_X^2$  distribution is measured in 39 bins in the range from 0 to  $13 \text{ GeV}^2/c^4$  (bin width  $0.333 \text{ GeV}^2/c^4$ ) and, after subtraction of all backgrounds, the finite detector resolution in  $M_X^2$  is unfolded using the Singular Value Decomposition (SVD) algorithm [22], as illustrated in Fig. 1. The

$p_{\min}^*$	$B^+$ electron	$B^+$ muon	$B^0$ electron	$B^0$ muon
0.7	$3893 \pm 79$ (72.3%)	$3626 \pm 84$ (68.7%)	$2212 \pm 64$ (66.4%)	$2154 \pm 64$ (65.0%)
0.9	$3659 \pm 75$ (74.0%)	$3484 \pm 78$ (71.1%)	$2072 \pm 58$ (66.4%)	$2067 \pm 58$ (70.2%)
1.1	$3285 \pm 70$ (75.2%)	$3159 \pm 73$ (72.9%)	$1886 \pm 53$ (66.4%)	$1925 \pm 52$ (76.1%)
1.3	$2742 \pm 64$ (75.9%)	$2740 \pm 66$ (75.0%)	$1595 \pm 46$ (66.4%)	$1632 \pm 47$ (79.4%)
1.5	$2152 \pm 56$ (77.7%)	$2132 \pm 56$ (76.8%)	$1195 \pm 39$ (66.4%)	$1297 \pm 41$ (83.0%)

TABLE I: Number of  $B \rightarrow X_c \ell \nu$  signal and signal purity in the four sub-samples, as a function of the lepton momentum threshold. The yields are quoted with their statistical uncertainty; the corresponding signal purity is given in brackets.

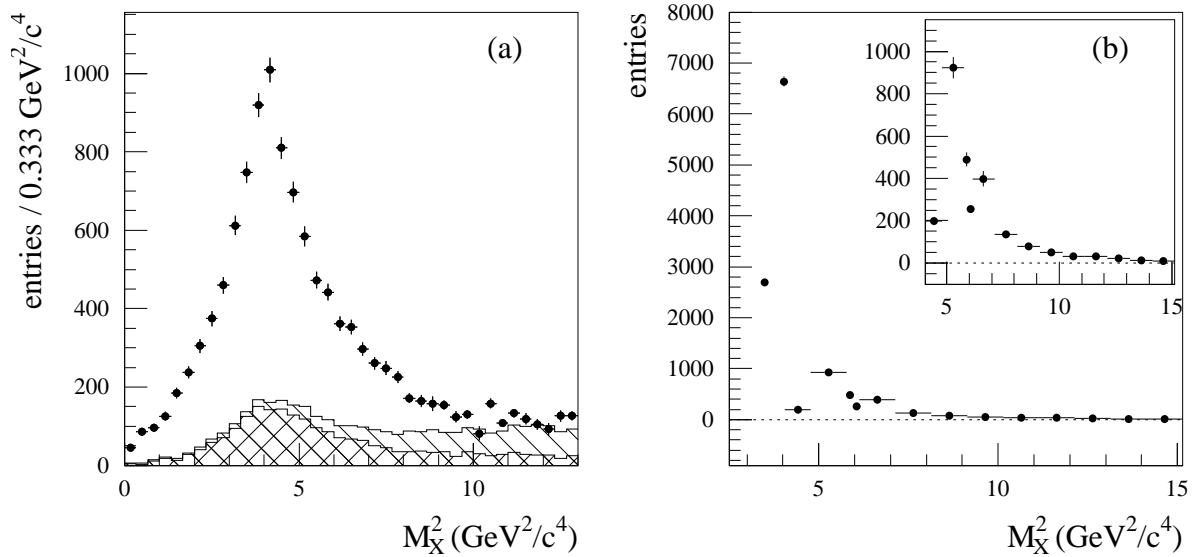


FIG. 1: (a) Measured and (b) unfolded  $M_X^2$  distribution for  $p_\ell^* > 0.7$  GeV/c. On the left plot, the continuum-subtracted  $M_X^2$  distribution is shown by points with error bars. The hatched histogram corresponds to the background from secondary or fake leptons;  $B\bar{B}$  events in which  $B_{\text{tag}}$  is misreconstructed are shown by the double-hatched histogram. The right plot is the result of the unfolding. In both plots, contributions from  $B^+$  and  $B^0$  tags, and from electron and muon events are added.

unfolded distribution has 15 bins in the range from  $M_D^2$  to about 15 GeV<sup>2</sup>/c<sup>4</sup> (bin width 1 GeV<sup>2</sup>/c<sup>4</sup>, except around the narrow states  $D$ ,  $D^*$ ,  $D_1$  and  $D_2^*$ ). We calculate the first and second moment,  $\langle M_X^2 \rangle$  and  $\langle (M_X^2 - \langle M_X^2 \rangle)^2 \rangle$ , for each unfolded  $M_X^2$  spectrum separately, after applying a small correction for different bin-to-bin efficiencies. The final results for a given lepton momentum threshold are obtained by taking the average over the four sub-samples. The unfolding, moment calculation and averaging procedure has been studied on MC simulated events and no significant bias has been found.

The results for the first and second hadronic mass moment are shown in Fig. 2 and Tables II and III. All results are preliminary. Note that the moment measurements for different lepton momentum thresholds are highly correlated due to overlapping data samples.

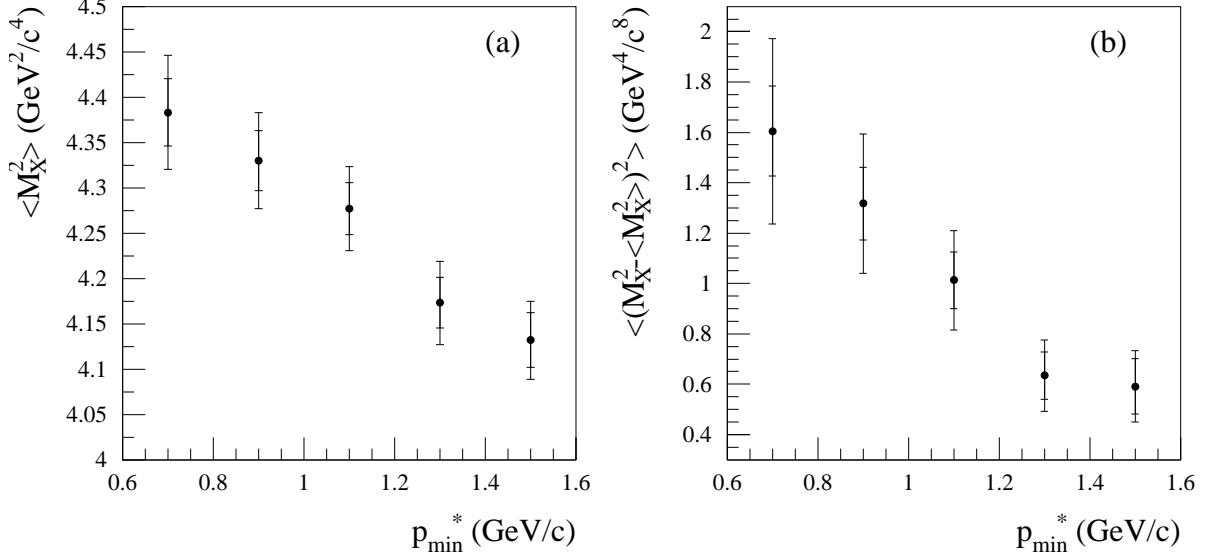


FIG. 2: (a) First and (b) second hadronic mass moment,  $\langle M_X^2 \rangle$  and  $\langle (M_X^2 - \langle M_X^2 \rangle)^2 \rangle$ , for different lepton threshold momenta. The error bars indicate the statistical and total errors. Note that the individual moments are highly correlated. All results are preliminary.

$p_{\min}^*$ (GeV/c)	$\langle M_X^2 \rangle$ (GeV <sup>2</sup> /c <sup>4</sup> )	detector/ background	unfolding	$X_c$ model
0.7	$4.383 \pm 0.037 \pm 0.051$	0.047	0.004	0.020
0.9	$4.330 \pm 0.033 \pm 0.041$	0.036	0.009	0.018
1.1	$4.277 \pm 0.029 \pm 0.035$	0.028	0.014	0.016
1.3	$4.173 \pm 0.028 \pm 0.037$	0.026	0.021	0.016
1.5	$4.132 \pm 0.030 \pm 0.031$	0.019	0.018	0.016

TABLE II: First hadronic mass moment  $\langle M_X^2 \rangle$  for different lepton threshold momenta. The first error on  $\langle M_X^2 \rangle$  is statistical and the second is the estimated systematic uncertainty. The right-most three columns show the different components of the systematic error. All results are preliminary.

We have estimated the correlations due to this overlap in Table IV.

We consider three sources of systematic error, shown separately in columns three to five of Tables II and III: the uncertainty related to the detector modeling and the background subtraction, the uncertainty related to unfolding and the moment extraction procedure, and the uncertainty related to the  $X_c$  model in the MC simulation. The total systematic error is the quadratic sum of these three components.

The uncertainty related to the detector modeling and the background subtraction is estimated by varying the normalizations of the different background components and some of the selections used in the analysis (namely the  $B_{\text{tag}}$  signal region and the requirement on  $M_{\text{miss}}^2$ ). The uncertainty related to unfolding and moment extraction is obtained by varying the effective rank parameter in the SVD algorithm, dis- and enabling the bin-to-bin efficiency

$p_{\min}^*$ (GeV/c)	$\langle(M_X^2 - \langle M_X^2 \rangle)^2\rangle$ (GeV <sup>4</sup> /c <sup>8</sup> )	detector/ background	unfolding	$X_c$ model
0.7	$1.605 \pm 0.179 \pm 0.322$	0.233	0.184	0.123
0.9	$1.317 \pm 0.144 \pm 0.236$	0.174	0.116	0.110
1.1	$1.013 \pm 0.113 \pm 0.161$	0.125	0.047	0.089
1.3	$0.634 \pm 0.095 \pm 0.105$	0.079	0.028	0.064
1.5	$0.591 \pm 0.110 \pm 0.088$	0.035	0.068	0.043

TABLE III: Same as Table II for the second hadronic mass moment  $\langle(M_X^2 - \langle M_X^2 \rangle)^2\rangle$ .

$p_{\min}^*$ (GeV/c)	$\langle M_X^2 \rangle$					$\langle (M_X^2 - \langle M_X^2 \rangle)^2 \rangle$					
	0.7	0.9	1.1	1.3	1.5	0.7	0.9	1.1	1.3	1.5	
$\langle M_X^2 \rangle$	0.7	1.000	0.922	0.807	0.620	0.533	0.782	0.720	0.622	0.471	0.415
	0.9		1.000	0.875	0.672	0.579	0.705	0.781	0.674	0.511	0.450
	1.1			1.000	0.768	0.661	0.561	0.622	0.770	0.583	0.514
	1.3				1.000	0.861	0.347	0.384	0.476	0.759	0.670
	1.5					1.000	0.342	0.379	0.470	0.749	0.778
$\langle (M_X^2 - \langle M_X^2 \rangle)^2 \rangle$	0.7						1.000	0.902	0.728	0.456	0.440
	0.9							1.000	0.807	0.506	0.487
	1.1								1.000	0.627	0.603
	1.3									1.000	0.963
	1.5										1.000

TABLE IV: Estimated correlation coefficients for the different moment measurements due to overlapping data samples.

correction and changing the binning of the unfolded distribution. The  $X_c$  model uncertainty is determined by varying the fractions of  $B \rightarrow D^* \ell \nu$ ,  $B \rightarrow D \ell \nu$  and  $B \rightarrow D^{**}/D^{(*)} \pi \ell \nu$  within  $\pm 10\%$ ,  $\pm 10\%$  and  $\pm 30\%$ , respectively, and summing the individual variations in quadrature. These ranges of variation roughly correspond to the experimental uncertainties [23] in the isospin averaged branching ratios.

In summary, we have measured the first and second moments of the hadronic invariant mass squared distribution,  $\langle M_X^2 \rangle$  and  $\langle(M_X^2 - \langle M_X^2 \rangle)^2\rangle$ , in  $B \rightarrow X_c \ell \nu$  decays for minimum lepton momenta ranging from 0.7 to 1.5 GeV/c in the  $B$  rest frame. The results obtained are compatible with theoretical expectations [1] and recent measurements from other experiments [6, 7]. In addition, we have estimated the correlations of the moment measurements. These measurements can be used as input to a global fit analysis, which is expected to lead to an improved determination of the CKM matrix element  $|V_{cb}|$ .

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